

July 20, 2000

Price and Quantity Competition among Heterogeneous Suppliers with Two-Part Pricing: Applications to Clubs, Local Public Goods, Networks, and Growth Controls

Yoshitsugu Kanemoto

Center for International Research on the Japanese Economy

Faculty of Economics, University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113 Japan

Abstract

Models of club goods, local public goods, and growth controls appear to have theoretical structures distinct from usual oligopoly models. This article shows, however, that they are special cases of a generalized oligopoly model that incorporates the possibility of two-part pricing and externalities between consumers (either congestion or network externalities). Our generalized two-part pricing model not only serves as a synthesis of a wide range of models but also allows us to obtain several new results on equilibrium prices. Another advantage of our model is that it can be interpreted as a reduced form of more complicated models that have spatial structures. This facilitates the extension to the case where firms are heterogeneous and the number of firms is arbitrary.

Keywords: two-part pricing; club theory; local public goods; growth controls; network externality

JEL classification: R4; D4; H7

Forthcoming in *Regional Science and Urban Economics*.

1. Introduction

Models of club goods, local public goods, and growth controls appear to have theoretical structures quite distinct from standard oligopoly models. This article shows, however, that they are special cases of a generalized oligopoly model that incorporates the possibility of two-part pricing and externalities between consumers (either congestion or network externalities). We thus offer a synthesis of many different types of models, including the private good models with or without network externalities, the shared facility model of Scotchmer (1985b), the club good models of Buchanan (1965), McGuire (1974), Berglas (1976), and Scotchmer (1985a), the local public good models of Stiglitz (1977), Wooders (1978), Kanemoto (1980), Wildasin (1980), Brueckner (1983), and Scotchmer (1986), and the urban growth control models of Epple et al. (1988), Brueckner (1990), Engle et al. (1992), Helsley and Strange (1995), Brueckner (1995), Sakashita (1995), and Brueckner and Lai (1996).

Our generalized two-part pricing model not only serves as a synthesis of a wide range of models but also allows us to obtain several new results on equilibrium prices. For example, if neither congestion nor network externality exists on the consumer side, then both access fees and unit prices are efficient under Bertrand-type price competition. In contrast, the profit maximizing access fee is distorted under Cournot-type quantity competition. We also show that the access fee is *lower* than the marginal social cost of an additional subscriber in the Bertrand case if network externalities exist.

Another advantage of our model is that it can be interpreted as a reduced form of more complicated models that have spatial structures. This facilitates the extension to the case where firms are heterogeneous and the number of firms is arbitrary.

As Oi (1971) has shown, two-part pricing eliminates monopolistic price distortion when consumers are homogeneous. Because a monopolist can use a lump-sum access fee to capture the consumer's surplus, he/she does not have to raise the unit price above the marginal cost. In an oligopoly setting access fees distort distribution of customers among different suppliers. This distortion is of a second-order magnitude, however, and Oi's result carries over to oligopoly models, as pointed out by Scotchmer (1985b). This feature of two-part pricing distinguishes our model from the standard oligopoly model.

With two-part pricing, potential choice variables for a firm are two types of prices, the access fee and unit prices, and two types of quantity variables, the number of customers and quantities of outputs. One can define different games, depending on which of these four are chosen as strategic variables. In this paper we restrict our attention to the case where a firm is a price taker concerning the access fee.¹ Concerning unit prices and quantities of outputs, we consider both price taking and quantity taking cases.

In both the price- and quantity-competition models, no distortion arises for the unit prices and capacity investment, but the access fee does not in general equal the marginal social cost of an additional subscriber. As the number of firms increases, the access fee approaches the marginal social cost. Even with a finite number of firms, however, a special case exists where the access fee is not distorted, i.e., a Bertrand equilibrium (a Nash equilibrium in prices) with neither congestion nor network externalities in consumption.

All the results in this paper follow from the first order conditions for profit maximization of a firm, with other firms' choice variables arbitrarily fixed. This

means that these results hold even if other firms are not maximizing profits. It is worth emphasizing that many of the qualitative results on equilibrium prices can be obtained without a full characterization of Nash equilibria. Our results are of course vacuous if a Nash equilibrium does not exist, and it is well known that it may not. It is also well known, however, that there are many cases where an equilibrium exists and our results are relevant in those cases.

The organization of this paper is as follows. Section 2 formulates an oligopoly model of two-part pricing. Section 3 examines price-taking behavior concerning unit prices, and Section 4 turns to the quantity taking case. Section 5 applies the results in Sections 3 and 4 to models of private goods, clubs, local public goods, and growth controls. Section 6 concludes the paper.

2. Model

Consider an oligopolistic, multiproduct market with two-part pricing. Although it is not difficult to extend our analysis to a differentiated oligopoly,² we restrict our attention to the homogeneous product case in order to avoid excessive notational complexity. The products (which we call goods X) may be club goods such as golf courses and tennis courts, local public services such as parks and roads, or network services such as telecommunication and electricity. Producers may differ in their cost structures but consumers are homogeneous. An extension to the heterogeneous consumer case is not trivial and left for future research.

Firms supply a vector of goods and services (denoted X), charging a lump-sum access fee (denoted f) and a vector of unit prices (denoted p). The cost function of the j -th firm is $C^j = C^j(X^j, n^j, k^j)$, where X^j is the output vector of the firm, n^j is

the number of subscribers, k^j is the capacity of the firm (or a capital input), and the cost function satisfies $C_X^j \equiv \partial C^j / \partial X^j > 0$, $C_n^j \equiv \partial C^j / \partial n^j \geq 0$, and $C_k^j \equiv \partial C^j / \partial k^j > 0$.

The assumption of $C_n^j \geq 0$ reflects the possibility that an increase in the number of subscribers is costly by itself. This is common in network industries where connecting a new user to a network requires additional facilities. For clubs and local public goods, an increase in membership may cause congestion even if the total consumption X^j is the same. For example, compare a tennis club with 100 members all of whom play one hour a day and another club with 50 members who play two hours a day. Although the total consumption measured by total hours of play is the same in the two cases, the former club would be more costly to operate because there are more people who use club facilities such as shower rooms.

The profits of firm j are $\Pi^j = f^j n^j + p^j X^j - C^j(X^j, n^j, k^j)$. We omit superscript j when this does not cause confusion.

All consumers have the same twice-differentiable and quasi-concave utility function, $U(z, x, X, n, k)$, where z is the consumption of the composite consumer good which represents all goods other than goods X ; x is a consumption vector of goods X ; and X , n , and k are respectively the output vector, the number of subscribers, and the capacity of the particular supplier that the consumer subscribes to. If x_i^j for $i=1, \dots, n^j$ is the consumption vector of the i -th customer of the j -th firm, we have

$$X^j = \sum_{i=1}^{n^j} x_i^j.$$

We assume that the first derivatives of the utility function satisfy $U_z > 0$,

$U_x > 0$, and $U_k \geq 0$. Goods X may involve congestion on the consumption side as well as the production side. Both the total consumption X and the number of subscribers n can cause congestion. In the tennis club example, the courts get crowded when the total hours of play increase, which results in $U_x \leq 0$. An increase in club members would lower utility even if the total hours X were the same, because shower rooms get more crowded. In this case, inequality $U_n \leq 0$ holds.

Note that in our model the capacity constraint can be 'soft.' The total consumption X can be increased without increasing 'capacity' k if consumers are willing to tolerate congestion. Our model however allows a strict capacity constraint as a limiting case. If for example the total consumption X can never exceed capacity k , then U_x is minus infinity at $X = k$.

Network externalities analyzed by Artle and Averous (1973), Littlechild (1975), Orens and Smith (1981), Rohlfs (1974), and Squire (1973) can be considered as "negative" congestion. In the case of telecommunication, a new subscriber gives external benefits to other subscribers because they now have the opportunity to call one more subscriber. We have $U_n \geq 0$ in this case.

Even in the presence of network externalities, more than one firm can coexist in equilibrium if congestion on the production side is strong enough to offset network externalities on the consumption side. This paper focuses on such a case.

A consumer may purchase goods X from more than one supplier, but under our assumption of homogeneous products nobody will do so in equilibrium because he/she can reduce the payment of access fees by trading with only one firm. From this and the homogeneous consumer assumption, we have $X = nx$ in equilibrium. A consumer,

however, takes X as given in his/her choice of x .

The budget constraint for a consumer is $y = z + f + px$, where y, f , and p are the consumer's income, an access fee, and a vector of unit prices of goods X respectively, and the composite consumer good is taken to be the numeraire.

Define the expenditure function

$$E(p, X, n, k, u) = \min_{\{z, x\}} \{z + px : U(z, x, X, n, k) \geq u\}. \quad (1)$$

Note that this expenditure function does not include the access fee. In equilibrium the budget constraint satisfies $y = f + E(p, X, n, k, u)$. We assume that the expenditure function is differentiable. The partial derivatives of the expenditure function then satisfy

$$E_X(p, X, n, k, u) = -U_X/U_z, \quad (2)$$

$$E_k(p, X, n, k, u) = -U_k/U_z < 0, \quad (3)$$

$$E_n(p, X, n, k, u) = -U_n/U_z, \quad (4)$$

$$E_u(p, X, n, k, u) = 1/U_z, \quad (5)$$

and

$$x(p, X, n, k, u) = E_p(p, X, n, k, u). \quad (6)$$

The last equation yields a recursive relationship,

$$X(p, k, n, u) = nx(p, X(p, k, n, u), n, k, u), \quad (7)$$

which defines a demand function that a firm is faced with. This reduced-form demand function satisfies

$$X_p = nx_p / (1 - nx_X) \quad (8)$$

$$X_n = (x + nx_n) / (1 - nx_X) \quad (9)$$

$$X_u = nx_u / (1 - nx_X). \quad (10)$$

We assume that $nx_x < 1$, $x + nx_n > 0$, and $x_u > 0$. The first two inequalities exclude perverse cases. If the first inequality does not hold, congestion externality is so strong that the demand curve that the firm is faced with is upward sloping in the unit price. It is the contraction condition that can be used to guarantee the existence of a unique fixed point of equation (7). The second inequality excludes the case where an increase in the number of subscribers reduces the total demand for X . The last inequality is equivalent to normality of goods X . Under these assumptions, we have $X_p < 0$, $X_n > 0$, and $X_u > 0$.

We assume that the total number of consumers is N and fixed. Because a consumer trades with one firm only, the population constraint,

$$\sum_{j=1}^J n^j = N, \quad (11)$$

must hold, where J is the number of firms. In equilibrium all consumers obtain the same utility level (denoted by u), which yields

$$E^j(p^j, X^j(p^j, k^j, n^j, u), n^j, k^j, u) = y - f^j, \quad j = 1, 2, \dots, J. \quad (12)$$

Models of private goods, club goods, local public goods, and growth controls are special cases of our model. These examples will be discussed in section 5.

3. Price Competition

This section examines price competition where each firm chooses its own prices to maximize profit, taking other firms' prices as given. A Nash equilibrium in prices (or a Bertrand equilibrium) is obtained when all firms simultaneously engage in this type of behavior. We do not, however, attempt a full characterization of a Nash equilibrium. All the results in this article are consequences of first order conditions for profit

maximization. Our results therefore hold so long as an interior optimum is obtained in equilibrium. An implication of this is that they do not require the usual Nash condition that other firms' prices are also optimally chosen. In particular, they hold even when other firms are not maximizing profits.

It is well known that a Nash equilibrium may not exist.³ In such a case, our results are vacuous, but we also know many examples where an equilibrium exists and our results are relevant in those cases. The uniqueness of the equilibrium is not always guaranteed, either, but our results hold for each equilibrium.

With two-part pricing, a firm chooses a price schedule that consists of the access fee f and unit prices p . In this section we assume that it takes both of them as given. The quantity competition that we examine in the next section assumes that a firm takes the access fee f and quantities X as given. The price competition applies when each firm believes that other firms fix their price schedules and satisfy whatever demand the price schedules generate. The quantity competition would be relevant when other firms are faced with strict capacity constraints so that even if the firm raises its price, they cannot respond by increasing supply.

Which of the two cases is more realistic depends on the structure of the technology and the market. For example, in the local public good model, the ownership structure of land may be an important determinant. If private individuals own land and land rent is determined by the market, land rent (which is one of the unit prices in our model as seen in Section 5) is not a direct choice variable for a local government (or a developer which supplies local public goods). In such a case a Cournot assumption is more appropriate. If a local government owns the land and sets the land rent, then a Bertrand assumption may be applicable although there is no a priori

reason to exclude the Cournot equilibrium even in this case.

In addition to these two variables, a firm can choose capacity k . If the capacity constraint is strict in the sense that k is an upper bound for the firm's production X , then it must adjust capacity k to meet whatever demand its price schedule generates. In such a case capacity k cannot be an independent choice variable. In our model with congestion, however, the firm can increase production X without expanding capacity k although the firm and consumers must incur congestion costs. In sum, each firm chooses the access fee f , the unit prices p , and capacity k , taking other firms' choices of these variables as given.

If prices and capacities of all firms are given, equilibrium conditions (11) and (12) yield the number of subscribers and the utility level,

$$n^j = n^j(\mathbf{f}, \mathbf{p}, \mathbf{k}), \quad j = 1, \dots, J, \quad (13)$$

$$u = u(\mathbf{f}, \mathbf{p}, \mathbf{k}), \quad (14)$$

where $\mathbf{f} = (f^1, \dots, f^J)$, $\mathbf{p} = (p^1, \dots, p^J)$, $\mathbf{k} = (k^1, \dots, k^J)$. Demand for firm j is then

$$X^j(p^j, k^j, n^j(\mathbf{f}, \mathbf{p}, \mathbf{k}), u(\mathbf{f}, \mathbf{p}, \mathbf{k})), \quad j = 1, \dots, J, \quad (15)$$

where $X^j(p^j, k^j, n^j, u)$ is the reduced form demand function derived in the preceding section.

Let us first consider profit maximization of firm 1 that takes other firms' policies, (f^2, \dots, f^J) , (p^2, \dots, p^J) , (k^2, \dots, k^J) , as given. Suppressing other firms' policies, we can rewrite (13) and (14) as

$$n^1 = n^1(f^1, p^1, k^1) \quad (16)$$

$$u = u(f^1, p^1, k^1). \quad (17)$$

The profit of firm 1 can then be written as a function of its choice variables (f^1, p^1, k^1) .

We can write this function as

$$\begin{aligned} \Pi(f, p, k) = & f n(f, p, k) + pX(p, k, n(f, p, k), u(f, p, k)) \\ & - C(n(f, p, k), X(p, k, n(f, p, k), u(f, p, k)), k) \end{aligned} \quad (18)$$

where we suppress superscript 1 when this does not cause confusion. Maximization of the profit function with respect to (f, p, k) yields the following first order conditions.

LEMMA 1. The first order conditions for profit maximization are

$$f - C_n = -\frac{1}{n_f} \{n + (p - C_X)(X_n n_f + X_u u_f)\} \quad (19)$$

$$p - C_X = -\frac{X + (f - C_n)n_p}{X_p + X_u u_p + X_n n_p} \quad (20)$$

$$(f - C_n)n_k + (p - C_X)(X_n n_k + X_k + X_u u_k) = C_k. \quad (21)$$

PROOF: Omitted.

These first order conditions represent a simple extension of the usual monopoly pricing formula. If the unit price equaled the marginal cost of production (i.e., $p = C_X$), then these conditions would be reduced to a monopoly pricing formula for the access fee f :

$$MC_n = MR_n = f \left(1 + \frac{n}{n_f f}\right) \leq f. \quad (22)$$

If the access fee equaled the marginal cost of a subscriber (i.e., $f = C_n$), then the same would hold for the unit prices p :

$$MC_X = MR_X = p \left(1 + \frac{X/p}{X_p + X_u u_p + X_n n_p}\right) \leq p. \quad (23)$$

In a monopoly model, Oi (1971) showed that the access fee is more efficient than the unit price in capturing the monopoly rent because it is a non-distortionary lump-sum charge. As noted by Scotchmer (1985b), this result extends to an oligopoly model. We show that distortion in unit prices does not occur in our model, either. It is

noteworthy that this is true even when access fees distort the distribution of customers between different suppliers.

Let us first evaluate the derivatives of $n^1(f^1, p^1, k^1)$ and $u(f^1, p^1, k^1)$.

LEMMA 2. Partial derivatives of $n^1(f^1, p^1, k^1)$ and $u(f^1, p^1, k^1)$ satisfy

$$n_f^1 = -\frac{1}{e_n^1} \frac{\sum_{j=2}^J (e_u^j / e_n^j)}{\sum_{j=1}^J (e_u^j / e_n^j)}; \quad u_f = -\frac{1}{e_n^1} \frac{1}{\sum_{j=1}^J (e_u^j / e_n^j)}$$

$$n_p^1 = (x^1 + E_X^1 X_p^1) n_f^1; \quad u_p = (x^1 + E_X^1 X_p^1) u_f$$

$$n_k^1 = (E_k^1 + E_X^1 X_k^1) n_f^1; \quad u_k = (E_k^1 + E_X^1 X_k^1) u_f$$

where

$$e_n^j = E_X^j X_n^j + E_n^j \quad \text{and} \quad e_u^j = E_X^j X_u^j + E_u^j \quad \text{for} \quad j = 1, \dots, J.$$

PROOF:

The derivatives of $n^1(f^1, p^1, k^1)$ and $u(f^1, p^1, k^1)$ follow from the total differentiation of equilibrium conditions (12) and (11),

$$\left[\begin{array}{c} \Omega \\ \left[\begin{array}{c} dn^1 \\ \vdots \\ dn^J \\ du \end{array} \right] \end{array} \right] = - \left[\begin{array}{c} 1 \\ 0 \\ \vdots \\ 0 \end{array} \right] df^1 - \left[\begin{array}{c} x^1 + E_X^1 X_p^1 \\ 0 \\ \vdots \\ 0 \end{array} \right] dp^1 - \left[\begin{array}{c} E_k^1 + E_X^1 E_k^1 \\ 0 \\ \vdots \\ 0 \end{array} \right] dk^1, \quad (24)$$

where

$$\Omega = \begin{bmatrix} e_n^1 & 0 & \dots & 0 & e_u^1 \\ 0 & e_n^2 & \ddots & \vdots & \vdots \\ \vdots & \ddots & \ddots & 0 & \vdots \\ 0 & \dots & 0 & e_n^J & e_u^J \\ 1 & \dots & 1 & 1 & 0 \end{bmatrix}. \quad (25)$$

Define

$$\omega = |\Omega| = - \left[\prod_{j=1}^J e_n^j \right] \sum_{j=1}^J \frac{e_u^j}{e_n^j} \quad (26)$$

$$\phi = \begin{vmatrix} 1 & 0 & \cdots & \cdots & 0 & e_u^1 \\ 0 & e_n^2 & 0 & \cdots & 0 & e_u^2 \\ \vdots & 0 & \ddots & \ddots & \vdots & \vdots \\ \vdots & \vdots & \ddots & \ddots & 0 & \vdots \\ 0 & 0 & \cdots & 0 & e_n^J & e_u^J \\ 0 & 1 & \cdots & 1 & 1 & 0 \end{vmatrix} \quad (27)$$

and

$$\psi = \begin{vmatrix} e_n^1 & 0 & \cdots & 0 & 1 \\ 0 & e_n^2 & \ddots & \vdots & 0 \\ \vdots & \ddots & \ddots & 0 & \vdots \\ 0 & \cdots & 0 & e_n^J & \vdots \\ 1 & \cdots & 1 & 1 & 0 \end{vmatrix} = - \prod_{j=2}^J e_n^j. \quad (28)$$

Then, by Cramer's rule, we obtain

$$n_f^1 = -\frac{\phi}{\omega} \quad \text{and} \quad u_f = -\frac{\psi}{\omega}, \quad (29)$$

which yields the first two equalities in the lemma. The rest of the lemma is obvious from (24). **Q.E.D.**

We can now show that distortion occurs only in the access fee, and the unit prices and capacity investment are not distorted.

PROPOSITION 1. If a firm maximizes its profit, taking the access fees, unit prices, and capacities of other firms as given, then its unit prices equal the marginal costs of producing goods X plus the marginal congestion costs,

$$p^j = C_X^j + n^j E_X^j, \quad j = 1, \dots, J,$$

and its capacity investment is carried out until the marginal benefit of capacity

expansion equals the marginal cost,

$$-n^j E_k^j = C_k^j, \quad j = 1, \dots, J.$$

The access fee diverges from the marginal social cost of a new subscriber:

$$f^j - C_n^j + n^j E_n^j = n^j \frac{E_u^j}{\sum_{i \neq j} (e_u^i / e_n^i)}, \quad j = 1, \dots, J.$$

PROOF:

Let us restrict our attention to $j = 1$ and suppress the superscript whenever this does not cause confusion. The same result holds for other firms. From Lemma 2, we have $n_p = (x + E_X X_p)n_f$, $u_p = (x + E_X X_p)u_f$, $n_k = (E_k + E_X X_k)n_f$, and $u_k = (E_k + E_X X_k)u_f$. Substituting these relationships into partial derivatives of the profit function (18) yields

$$\Pi_p = (x + E_X X_p)\Pi_f + (p - C_X - nE_X)X_p, \quad (30)$$

and

$$\Pi_k = (E_k + E_X X_k)\Pi_f + (p - C_X - nE_X)X_k - (nE_k + C_k). \quad (31)$$

Combining these relationships with the first order conditions for profit maximization (i.e., $\Pi_f = \Pi_p = \Pi_k = 0$) shows that, if $X_p \neq 0$, then $p = C_X + nE_X$ and $-nE_k = C_k$.

Next, from Lemma 2 and

$$\Pi_f = n + \{(f - C_n) + (p - C_X)X_n\}n_f + (p - C_X)X_u u_f = 0, \quad (32)$$

we obtain

$$\begin{aligned}
f &= C_n - nE_X X_n - \frac{n}{n_f} (1 + E_X X_u u_f) \\
&= C_n - n(e_n^1 - E_n^1) + ne_n^1 \frac{\sum_{j=1}^J (e_u^j / e_n^j)}{\sum_{j=2}^J (e_u^j / e_n^j)} \left[1 + (e_u^1 - E_u^1) \left(-\frac{1}{e_n^1} \frac{1}{\sum_{j=1}^J (e_u^j / e_n^j)} \right) \right] \quad (33) \\
&= C_n + nE_n^1 + n \frac{1}{\sum_{j=2}^J (1/e_n^j)(e_u^j / E_u^1)}
\end{aligned}$$

where we used the relationships, $e_n^j = E_X^j X_n^j + E_n^j$ and $e_u^j = E_X^j X_u^j + E_u^j$, in Lemma 2 in deriving the second equality.

Q.E.D.

The distortion in the access fee is a result of the pecuniary or migration externality emphasized by Scotchmer (1986) in the context of local public goods. Any action of a jurisdiction that benefits its residents induces new immigration. The jurisdiction is faced with a downward sloping demand curve because the immigration lowers land prices in other jurisdictions. The jurisdiction raises the access fee to exploit the monopoly power from this migration externality. Instead of raising the access fee, it could raise unit prices or reduce capacity investment (which corresponds to the supply of local public goods in the local public good model), but the access fee is a more efficient tool to extract the consumer surplus. If the access fee is assumed impossible as common in the local public good literature, the supply of local public goods will be distorted, as shown by Scotchmer (1986).

The following corollary shows a surprising result that there exists a case where no distortion occurs for the access fee as well as unit prices.⁴

COROLLARY 1. If neither congestion nor network externality exists on the consumer side (i.e., $U_x = U_n = 0$), then the access fee equals the social marginal cost of an additional subscriber, i.e., $f^j = C_n^j$ for any j .

This corresponds to the well-known result that in a Bertrand model the price equals the marginal cost. Because we assumed that a firm takes other firms' access fees as given, it is faced with a horizontal demand curve (i.e., $n_f = -\infty$) if no externality exists on the consumption side.

Congestion on the consumer side makes the demand curve downward sloping. The reason is that, because adding customers means more severe congestion, the firm must reduce the access fee to attract more customers. With a downward sloping demand curve, the profit maximizing level of access fee exceeds the marginal social cost of an additional subscriber.

The network externality has the opposite effect of making the demand curve upward sloping. If $U_n > 0$ and $U_x = 0$, then raising the access fee increases the number of subscribers (i.e., $n_f > 0$). The above proposition shows that the access fee is lower than the marginal social cost of a subscriber in this case. Note that the second order condition for profit maximization is satisfied even in this case if congestion on the production side raises the firm's costs sufficiently to offset the increase in revenue caused by raising the access fee.

COROLLARY 2. If $U_x \leq 0$ and $U_n \leq 0$, then the access fee is higher than or equal to the marginal social cost of an additional subscriber:

$$f^j \geq C_n^j + n^j E_n^j, \quad j = 1, \dots, J.$$

If $U_n > 0$ and $U_x = 0$, then the access fee is lower than the marginal social cost.

If $U_x > 0$ and $U_n > 0$, then it is not clear whether or not the access fee is lower than the social marginal cost because e_u may become negative.

Although the access fee is in general distorted, the total number of subscribers is fixed at N and will not be distorted. Distortions in real resource allocation are therefore limited to the distribution of subscribers among firms.

The formula for the access fee becomes simpler in a symmetric equilibrium where all firms have the same cost structure and charge the same price.

COROLLARY 3. In a symmetric equilibrium, we have

$$f - C_n - nE_n = \frac{1}{J-1} n(E_x X_n + E_n) \frac{E_u}{E_x X_u + E_u}.$$

This corollary implies that, as the number of firms becomes larger, the access fee approaches the social marginal cost of a subscriber. The distortion in access fee is proportional to $1/(J-1)$. For example, the distortion becomes a half as the number of firms increases from 2 to 3. In our model the first best allocation is attained in the symmetric case. Because all consumers purchase goods X and the number of consumers is fixed, the access fees are equivalent to non-distortionary lump-sum taxes so long as all firms charge equal fees.

4. Quantity Competition

In this section we consider a Cournot case where a firm maximizes its profit, taking the access fees (f^j 's) and outputs (X^j 's) of other firms as given. This case is relevant if it takes time for other firms to change the access fee and outputs while the

number of customers and unit prices change quickly. As noted in the preceding section, a typical example would be a local public good model where private individuals own land and the local government levies taxes on land rent.

Consider profit maximization of firm 1 that takes other firms' policies, (f^2, \dots, f^J) , (X^2, \dots, X^J) , (k^2, \dots, k^J) , as given. Solving $X^j = X(p^j, k^j, n^j, u)$ for p^j , we obtain $p^j = p^j(X^j, k^j, n^j, u)$. Using this relationship, we can rewrite the market clearing condition (12) as

$$E^j(p^j(X^j, k^j, n^j, u), X^j, n^j, k^j, u) = y - f^j, \quad j = 1, 2, \dots, J. \quad (34)$$

Then, in the same way as in the preceding section, we can write the number of subscribers and their utility level as functions of firm 1's choice variables:

$$n^1 = n^1(f^1, X^1, k^1) \quad (35)$$

$$u = u(f^1, X^1, k^1). \quad (36)$$

Firm 1 maximizes

$$\Pi^1 = f^1 n^1 + p^1(X^1, k^1, n^1, u) X^1 - C^1(n^1, X^1, k^1) \quad (37)$$

with respect to (f^1, X^1, k^1) subject to (35) and (36). We suppress superscript 1 when obvious.

The next lemma obtains the derivatives of (35) and (36).

LEMMA 3. Partial derivatives of $n^1(f^1, X^1, k^1)$ and $u(f^1, X^1, k^1)$ satisfy

$$n_f^1 = -\frac{1}{e_n^1} \frac{\sum_{j=2}^J (e_u^j / e_n^j)}{\sum_{j=1}^J (e_u^j / e_n^j)}; \quad u_f = -\frac{1}{e_n^1} \frac{1}{\sum_{j=1}^J (e_u^j / e_n^j)}$$

$$n_X^1 = (xp_X + E_X) n_f; \quad u_X = (xp_X + E_X) u_f$$

$$n_k^1 = (E_k + xp_k)n_f; \quad u_k = (E_k + xp_k)u_f.$$

PROOF:

If we replace elements of Ω in the preceding section by

$$e_n^j = x^j p_n^j + E_n^j = -x^j \frac{X_n^j}{X_p^j} + E_n^j,$$

$$e_u^j = x^j p_u^j + E_u^j = -x^j \frac{X_u^j}{X_p^j} + E_u^j \geq 0,$$

then we obtain

$$\left[\begin{array}{c} \Omega \\ \left[\begin{array}{c} dn^1 \\ \vdots \\ dn^J \\ du \end{array} \right] \end{array} \right] = - \left[\begin{array}{c} 1 \\ 0 \\ \vdots \\ 0 \end{array} \right] df^1 - \left[\begin{array}{c} x^1 p_X^1 + E_X^1 \\ 0 \\ \vdots \\ 0 \end{array} \right] dX^1 - \left[\begin{array}{c} E_k^1 + x^1 p_k^1 \\ 0 \\ \vdots \\ 0 \end{array} \right] dk^1.$$

The lemma then immediately follows by applying the same argument as in Lemma 2.

Q.E.D.

Equilibrium prices can be characterized in the same way as in the preceding section.

PROPOSITION 2. If a firm maximizes its profit, taking the access fees, output levels, and capacities of other firms as given, then unit prices and capacity investment satisfy the same conditions as in the price competition case. The condition for the access fee is also the same as in Proposition 1 if e_n^j and e_u^j are modified as

$$e_n^j \equiv -x^j \frac{X_n^j}{X_p^j} + E_n^j \quad \text{and} \quad e_u^j \equiv -x^j \frac{X_u^j}{X_p^j} + E_u^j.$$

PROOF:

From Lemma 3,

$$\Pi_X = (xp_x + E_X)\Pi_f + (p - C_X - nE_X)$$

$$\Pi_k = (xp_k + E_X)\Pi_f - (nE_k + C_k).$$

Hence, the first order conditions for profit maximization, $\Pi_f = \Pi_X = \Pi_k = 0$, yield

$$p = C_X + nE_X \quad \text{and} \quad -nE_k = C_k.$$

Now, from

$$\Pi_f = n + (f - C_n + Xp_n)n_f + Xp_u u_f = 0,$$

we get

$$f = C_n + nE_n + n^1 \frac{1}{\sum_{j=2}^J (1/e_n^j)(e_u^j/E_u^1)}.$$

Q.E.D.

Thus, no distortion arises in unit prices and capacity investment also in the quantity competition case. The access fee is distorted as in the Bertrand equilibrium but the precise formulae are different.

An important difference from the Bertrand case is that distortion in the access fee does not vanish even when neither congestion nor network externality exists on the consumer side.

COROLLARY 4. Even if $E_X^j = E_n^j = 0$, the access fee exceeds the social marginal cost of an additional subscriber: $f^j > C_n^j$.

Because a firm takes other firms' unit prices and access fee as given in a Bertrand model, a slight rise in its access fee (with unit prices fixed) induces a mass exodus of its customers. In a Cournot model, however, it takes other firms' output levels as fixed

and believes that their unit prices will be adjusted to meet the market clearing condition. In such a case a small rise in the access fee induces only a small reduction in the number of customers.

Another implication of Proposition 2 is that the access fee can be higher than the marginal social cost of an additional subscriber even in the case of network externality.

COROLLARY 5. Even if $U_n > 0$ and $U_x = 0$, the access fee can exceed the marginal social cost of an additional subscriber.

In a symmetric equilibrium we obtain the following corollary.

COROLLARY 6. In a symmetric equilibrium we have

$$f = C_n + nE_n + \frac{1}{J-1} \frac{E_u \left[-X \left(\frac{X_n}{X_p} \right) + nE_n \right]}{-x \left(\frac{X_u}{X_p} \right) + E_u}.$$

As in the Bertrand case, the distortion in the access fee will vanish as the number of firms approaches infinity. Even if the access fee is distorted, however, a symmetric equilibrium is first best efficient, since the total number of consumers is fixed.

5. Examples: Private Goods, Clubs, Local Public Goods, Networks, and Growth Controls

Models of private goods, club goods, local public goods, and growth controls are special cases of our model.

5.1. Private Goods

A private good model assumes a utility function $U(z, x)$ and a cost function $C(X)$. With two-part pricing the budget constraint for a consumer is $y = z + f + px$.

In the private good case, we have $U_X = U_n = U_k = 0$, $E_X = E_n = E_k = 0$, and $C_n = C_k = 0$. Substituting these relationships into Propositions 1 and 2 yields $p = C_X$ and $f = 0$ under Bertrand competition, and $p = C_X$ and

$$f = -\frac{1}{J-1} \frac{(x)^2}{x_p} \frac{E_u}{-x(X_u/X_p) + E_u}$$

under Cournot competition. The unit price therefore equals the marginal cost in both cases. The access fee equals the social marginal cost of an additional subscriber (which is zero in this case) only in the Bertrand case. In the Cournot case, the access fee exceeds the social marginal cost except in the limit as the number of firms approaches infinity.

5.2. Club Goods:

(a) A fixed use intensity model

Club models of the simplest type assume that the consumption of the club good, x , is fixed exogenously. This fixed use intensity model is a special case of our model with utility function $U(z, n, k)$ and cost function $C(k)$. Because the consumption of the club good is fixed exogenously in this case, we can safely assume that the unit price is zero. A firm charges only the access fee (membership fee), and the budget constraint is $y = z + f$.

In this case, we have $U_X = 0$, $E_X = 0$, and $C_n = 0$. Substituting these relationships into Propositions 1 and 2 yields $-nE_k = C_k$ and $f = \frac{J}{J-1} nE_n$ in both the Bertrand and Cournot cases. The marginal benefit of capacity expansion equals the marginal cost. The membership fee (the access fee) is positive because an increase in membership causes congestion. When the number of clubs is two, the access fee is

twice as high as the congestion cost of an additional club member. The access fee quickly approaches the marginal congestion cost as the number of clubs increases.

(b) Variable use intensity and shared facility models

The variable use intensity model in Berglas (1976) assumes a utility function $U(z, x, X, k)$ and a cost function $C(k, X)$. The shared facility model of Scotchmer (1985b) assumes congestion only on the consumption side: the utility function is $U(z, x, X)$ and the cost of the facility is fixed. Suppliers adopt two-part pricing and the budget constraint for a consumer is $y = z + f + px$. In both cases, an increase in club members does not cause congestion so long as the total congestion, X , is constant. We therefore have $U_n = 0$, $E_n = 0$, and $C_n = 0$.

First, in the Bertrand case the access fee is

$$f = \frac{1}{J-1} nE_X \frac{x}{1-nx_X} \frac{E_u}{E_X X_u + E_u}$$

for both the variable use intensity and shared facility models. Because an additional user of a facility does not cause any increase in social costs so long as the total consumption X is the same, the efficient level of the access fee is zero. With a finite number of firms, the access fee is positive, but it approaches zero as the number increases.

The unit price is $p = C_X + nE_X$ in a variable use intensity model and $p = nE_X$ in a shared facility model. The unit price equals the marginal congestion cost of X .

If the utility function is quasi-linear as in Scotchmer (1985b), then $X_u = 0$ and $x_X = 0$, which yields $f = \frac{1}{J-1} xp$ in the shared facility model. This coincides with Scotchmer's result. In this case the access fee happens to equal the revenue from unit

prices, i.e., $f = px$, when the number of firms is two.

Next, the Cournot equilibrium has the same unit price as the Bertrand equilibrium. The access fee is

$$f = -\frac{1}{J-1} \frac{(x)^2}{x_p} \frac{E_u}{-x(X_u/X_p) + E_u},$$

which is different from that in the Bertrand equilibrium.

5.3. Local Public Goods:

The local public good model of McGuire (1974), Wildasin (1980), Brueckner (1983), and Scotchmer (1986) assumes that a consumer must purchase residential land to consume local public goods. If we interpret x and k as land and local public goods respectively, the local public good model is a special case of our model with utility function $U(z, x, k)$ and cost function,

$$C(k, X) = \begin{cases} C(k) & \text{if } X \leq H \\ \infty & \text{if } X > H \end{cases}$$

where H is the total available land in a jurisdiction.

Except in Scotchmer (1986), the head tax (or the access fee) is assumed impossible and local public goods are financed by a (100%) tax on land rent. The budget constraint for a consumer is then $y = z + px$; and the 'profit' of a local government is the total land rent minus the cost of the public good, $pH - C(k)$. If the head tax is available, the budget constraint becomes $y = z + f + px$. The 'profit' of a local government in this case is $pH + fn - C(k)$.

First, consider the Bertrand case where the unit price, i.e., land rent, is a strategic variable. This case may be justified if a local government owns all the land in its jurisdiction and sets the head tax and land rent to maximize its fiscal surplus, i.e., the

sum of the head tax and land rent revenues minus the cost of local public goods.

Since $U_x = U_n = C_n = 0$, we have $p = U_x/U_z$, $n(U_k/U_z) = C_k$ and $f = 0$.

Thus there is no distortion in land rent, capacity investment, and the head tax even if the number of local governments is finite: the land rent is equal to the marginal rate of substitution between land and the consumer good, the marginal benefit of capacity expansion equals the marginal cost, and the head tax (or the access fee) is zero.

The last result is obtained because no externality exists on the consumption side (i.e., $U_x = U_n$) and the marginal cost of membership is zero (i.e., $C_n = 0$). This implies that in the Bertrand case the head tax is not necessary to attain the efficient supply of local public goods. This result depends crucially on our Bertrand assumption. We shall see below that in a Nash equilibrium in quantities the head tax is positive.

Unlike in the Bertrand case, the head tax is positive in the Cournot case:

$$f = -\frac{1}{J-1} \frac{(x)^2}{x_p} \frac{E_u}{-x(X_u/X_p) + E_u}.$$
 An implication of this is that if the head tax is restricted to zero, the unit price and/or capacity choice will be distorted.⁵ If the utility function is quasi-linear, then $X_u = 0$ and we obtain the same result as in Scotchmer (1986):

$$f = -\frac{1}{J-1} \frac{(x)^2}{x_p}.$$

In the limit as the number of firms approaches infinity, the access fee becomes zero. There is an extensive literature on this case, e.g., Brueckner (1983), Kanemoto (1980), and Henderson (1985). An important issue that is treated in this literature is whether a property tax on housing serves as a congestion tax. Consider an extension of the (pure) local public good model to allow for congestion, i.e., the cost function is now

$C(k, n, X)$. Then, the first best allocation requires the access fee (or the head tax) as a congestion tax. Hamilton (1975) shows that the property tax on housing consumption serves as a congestion fee. His result however relies on zoning regulation that correct the distortion in housing consumption caused by the property tax. Hoyt (1991), Krelove (1993), and Wilson (1997) examine whether the property tax can serve as a congestion fee even when there are no zoning restrictions on zoning. This issue may be analyzed in our framework by assuming that the output vector consists of two components, land and housing. We do not spell out the results here because they coincide with Wilson's.

5.4. *Growth Controls*

Models of growth controls typically have a spatial dimension. The effect of the regulation is to restrict the physical size of the city. Examples of these models are in Epple et al. (1988), Brueckner (1990), Engle et al. (1992), Helsley and Strange (1995), Brueckner (1995), Sakashita (1995), and Brueckner and Lai (1996). Here we use the framework of Helsley and Strange (1995).

They assume that each community occupies a linear strip of land with a unit width and that each household consumes one unit of land. Everybody commutes to the Central Business District (CBD) located at the left edge of the strip. Under these assumptions the population of a community, denoted n , coincides with the length of the residential zone. Commuting costs per unit distance is t . The utility function of a household is $u = \tilde{z} + a(n)$, where \tilde{z} is the composite consumer good and $a(n)$ represents the amenity level that depends on the population size. We use the notation \tilde{z} because the conversion of this spatial model into our non-spatial framework requires a change of variable, as will be seen later. Helsley and Strange fully characterize Nash

equilibria assuming that the amenity function has a linear form, $a(n) = -an$. The opportunity costs of the residential land are zero so that if there is no growth control, the residential land rent at the edge of the city is also zero. Growth controls raise this boundary land rent to a positive level.

All residents in a community receive the same utility level in equilibrium. This allows us to convert the spatial model into our non-spatial framework by focusing on a resident at the edge of the city. Because the length of the residential zone is n , the commuting costs for this resident are tn . Consider a growth control that raises the land rent at the edge from zero to f . The budget constraint for the resident is then $y = \tilde{z} + tn + f$. Now, we redefine the consumer good as $z = \tilde{z} + tn$. The budget constraint is then $y = z + f$ and the utility function is $U(z, x, X, n, k) = z - an - tn$.

The per-capita cost of public service provision is a constant c . The community developer receives the land rent in the residential zone that equals $fn + \frac{t}{2}n^2$. The profit of a community developer is then $\pi = (f - c)n + \frac{t}{2}n^2$. In our non-spatial framework, the cost function of public services that is compatible with this profit function is $C(n, X, k) = cn - \frac{t}{2}n^2$.

Thus, the non-spatial counterpart of the growth control model has congestion on the consumer side represented by the last term in the utility function and an offsetting scale economy on the production side represented by the last term in the cost function. These properties will play a crucial role in creating inefficiencies of growth controls.

In the growth control model of Helsley and Strange (1995), the levels of local public services X are exogenous and their prices p do not exist. Their price control game assumes that a community takes the access fees (rather than unit prices) of other

communities as given, whereas in their population control game populations of other communities are taken as given. We restrict our attention to the first game but it is not difficult to extend the analysis to the second game.

In the analysis of the price competition game, Helsley and Strange (1995) assumes that two active communities engage in price controls and that a passive community sets the price equal to zero. In our model, this corresponds to the case where the active communities choose the access fee f optimally, taking other communities' access fees fixed. Substituting the utility function

$U(z, x, X, n, k) = z - an - tn$ and the cost function $C(n, X, k) = cn - \frac{t}{2}n^2$ into

Proposition 1 yields $f = c + \frac{(3a+t)n}{2}$ for an active community, where n is the

population of the community. This shows that a community's choice of growth control is always inefficient because the 'price' for entry exceeds the per capita cost of local public services, i.e., $f > c$.

Note that the inefficiency result holds even if the population size does not affect the amenity level. The reason is that an increase in population size results in higher commuting costs. Although the utility function in the original spatial model does not contain commuting disutilities, the utility function in the non-spatial counterpart embodies a change in commuting costs induced by an increase in population.

Helsley and Strange obtain the full characterization of the Nash equilibrium and

show, in our notation, that $n = \frac{2[(a+t)N - c]}{9a + 7t}$ and $f = \frac{(a+t)[6c + (3a+t)N]}{9a + 7t}$. This

is consistent with our results.

6. Concluding Remarks

With two-part pricing, many of the results in oligopoly theory must be modified. The most important modification is that, with homogeneous consumers, unit prices and capacity investment are not distorted even when a firm has monopoly power. The access fee is distorted, but the distortion disappears as the number of firms increases.

Scotchmer (1985b) obtained these results in a Bertrand equilibrium of a simple shared facility model. This paper extends the results to Bertrand and Cournot equilibria of a fairly general model with heterogeneous suppliers. Our model includes private goods, club goods, local public goods, shared facilities, and growth controls as special cases. This extension clarifies relationships among these models and between the two types of equilibria. Furthermore, we obtain interesting new results. For example, if there is neither congestion nor network externality on the consumption side, a Bertrand equilibrium involves no distortion even in the access fee. The local public good model is an important example of this case. Another interesting result is that network externalities on the consumption side tend to make the access fee *lower* than the social marginal cost of an additional subscriber.

We assumed that the profits of the firms are given to absentee shareholders. If the consumers own the shares of the firms, then repercussions through distribution of profit income are introduced. The analysis of such a case is somewhat more complicated, but similar (though more complicated) formulas are obtained. All the qualitative results remain the same.

The assumption of homogeneous consumers is crucial to our results. With heterogeneous consumers, the analysis becomes much more complicated because the

price structure serves an additional role of a self-selection device. Much of the literature on nonlinear pricing in a monopoly model focused on this aspect, and extending their results to oligopolistic competition is a fruitful direction of future research.⁶

Acknowledgement

The Summer Workshop on Network Economics at Hokkaido University held in July 1990 stimulated my interest in oligopolistic competition with two-part pricing. I would like to thank the participants of the workshop, especially Professor Godfroy Dang'Nguyen, for useful presentations and discussions. I also thank the two referees and the participants of the workshops at the University of Tokyo, the Institute for Social and Economic Research of Osaka University, the University of Mannheim, and Kyoto University for helpful comments. Support from Grants in Aid for Scientific Research of Ministry of Education in Japan, the JSPS Research for the Future Program, and the Research Project on the Role of the Government in Network Industries at the Center for International Research on the Japanese Economy is gratefully acknowledged.

References

- Artle, R. and C. Averous, 1973, The Telephone System as a Public Good: Static and Dynamic Aspects, *The Bell Journal of Economics and Management Science* 4, 89-100.
- Berglas, E., 1976, On the Theory of Clubs, *American Economic Review* 66, 116-121.
- Brown, S. J. and D.S. Sibley, 1986, *The Theory of Public Utility Pricing* (Cambridge University Press, Cambridge).
- Brueckner, J., 1983, Property Value Maximization and Public Sector Efficiency, *Journal*

- of Urban Economics 14, 1-15.
- Brueckner, J., 1990, Growth Controls and Land Values in an Open City, *Land Economics* 66, 237-248.
- Brueckner, J., 1995, Strategic Control of Growth in a System of Cities, *Journal of Public Economics* 57, 393-416.
- Brueckner, J.K. and F-C. Lai, 1996, Urban Growth Controls with Resident Landowners, *Regional Science and Urban Economics* 26, 125-143.
- Buchanan, J., 1965, An Economic Theory of Clubs, *Economica* 32, 1-14.
- Calem, P.S. and D.F. Spulber, 1984, Multiproduct Two Part Tariffs, *International Journal of Industrial Organization* 2, 105-115.
- Engle, R., P. Navarro, and R. Carson, 1992, On the Theory of Growth Controls, *Journal of Urban Economics* 32, 269-284.
- Epple, D., T. Romer, and R. Filimon, 1988, Community Development with Endogenous Land Use Controls, *Journal of Public Economics* 35, 133-162.
- Hamilton, B.W., 1975, Zoning and Property Taxation in a System of Local Governments, *Urban Studies* 12, 205-211.
- Helsley, R.W. and W.C. Strange, 1995, Strategic Growth Controls, *Regional Science and Urban Economics* 25, 435-460.
- Henderson, J.V., 1985, The Tiebout Hypothesis: Bring Back the Entrepreneurs, *Journal of Political Economy* 93, 249-264.
- Hoyt, W.H., 1991, Competitive Jurisdictions, Congestion, and the Henry George Theorem: When Should Property Be Taxed Instead of Land, *Regional Science and Urban Economics* 21, 351-370.
- Kanemoto, Y., 1980, *Theories of Urban Externalities* (North-Holland, Amsterdam).

- Krelove, R., 1993, The Persistence and Inefficiency of Property Tax Finance of Local Public Expenditures, *Journal of Public Economics* 51, 415-435.
- Littlechild, S.C., 1975, Two-Part Tariffs and Consumption Externalities, *Bell Journal of Economics* 6, 661-670.
- McGuire, M., 1974, Group Segregation and Optimal Jurisdictions, *Journal of Political Economy* 82, 112-132.
- Oi, W.Y., 1971, A Disneyland Dilemma: Two-Part Tariffs for a Mickey Mouse Monopoly, *Quarterly Journal of Economics* 85, 77-96.
- Orens, S.S. and S.A. Smith, 1981, Critical Mass and Tariff Structure in Electronic Communications Market, *Bell Journal of Economics* 12, 467-487.
- Rohlf, J., 1974, A Theory of Interdependent Demand for a Communications Service, *The Bell Journal of Economics and Management Science* 5, 16-37.
- Sakashita, N., 1995, An Economic Theory of Urban Growth Control, *Regional Science and Urban Economics* 25, 427-434.
- Scotchmer, S., 1985a, Profit Maximizing Clubs, *Journal of Public Economics* 27, 25-45.
- Scotchmer, S., 1985b, Two-Tier Pricing of Shared Facilities in a Free-Entry Equilibrium, *Rand Journal of Economics* 16, 456-472.
- Scotchmer, S., 1986, Local Public Goods in an Equilibrium, *Regional Science and Urban Economics* 16, 463-481.
- Squire, L., 1973, Some Aspects of Optimal Pricing for Telecommunications, *The Bell Journal of Economics and Management Science* 4, 515-525.
- Stiglitz, J.E., 1977, The Theory of Local Public Goods, in: Feldstein, M.S. and R.P. Inman, eds., *The Economics of Public Services* (Macmillan, London), 274-333.
- Wildasin, D.E., 1980, Locational Efficiency in a Federal System, *Regional Science and*

Urban Economics 10, 453-471.

Wilson, J.D., 1997, Property Taxation, Congestion, and Local Public Goods, Journal of Public Economics 64, 207-217.

Wooders, M., 1978, Equilibria, the Core and Jurisdiction Structures in Economies with a Local Public Good, Journal of Economic Theory 18, 328-348.

Footnotes

- ¹ It is not difficult to analyze quantity-taking behavior concerning the number of customers, but, in our model where all consumers are homogeneous and the total number of consumers is fixed, a firm is faced with a fixed number of customers if those of the rest of the firms are fixed. In order to obtain a non-trivial equilibrium we have to allow for endogenous population size or to assume that some communities fix the access fees rather than quantities. Helsley and Strange (1995) adopts the latter approach assuming that one of the communities is passive, i.e., fixes the access fee at zero.
- ² See Calem and Spulber (1984) for the analysis of a differentiated oligopoly model with two-part pricing.
- ³ See Stiglitz (1977) for an elementary illustration of the possibility of non-existence of a competitive equilibrium in the local public good model.
- ⁴ Note that the absence of congestion on the consumer side does not necessarily imply natural monopoly because congestion on the production side tends to favor smaller firm size.
- ⁵ Scotchmer (1986) obtained this result in a local public good model.
- ⁶ See Brown and Sibley (1986) for an excellent textbook treatment of nonlinear pricing with heterogeneous demand.